



# Helping With Math

## Understanding Properties and Hierarchy of Shapes

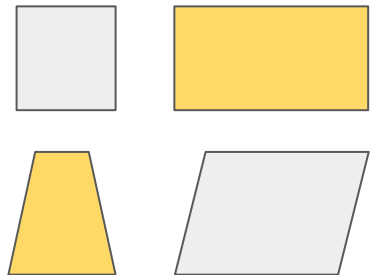
**GRADE 5**



Some quadrilaterals also possess the definitions of other quadrilaterals. It is just that these quadrilaterals have even more limitations. For instance, a rectangle is a type of parallelogram with congruent angles.

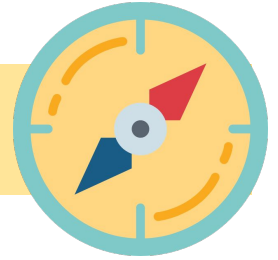


Today, we will be learning about the properties and hierarchy of shapes. Do you remember the different types of quadrilaterals? What are they?

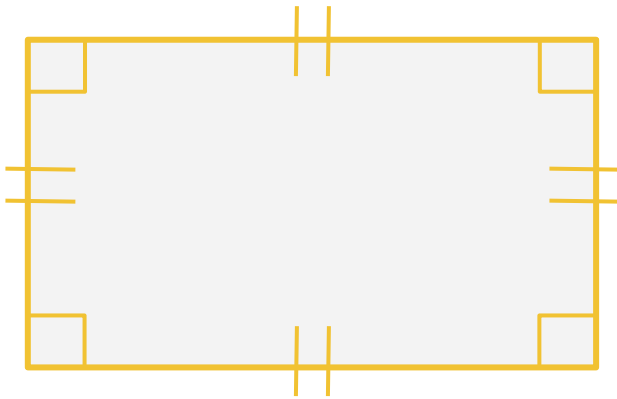


# PROPERTIES OF SHAPES

QUADRILATERAL is a closed figure with four sides.



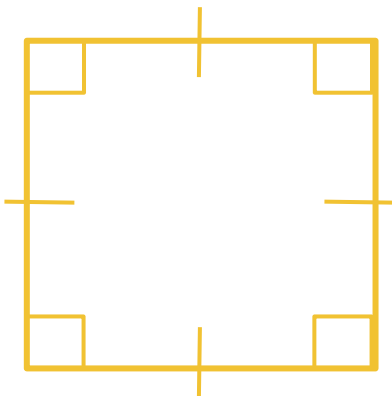
## RECTANGLE



**Rectangle is a quadrilateral with:**

- four right angles, meaning four 90-degree angles
- equal opposite sides

## SQUARE



**Square is a quadrilateral with:**

- four right angles, meaning four 90-degree angles
- four equal sides



# PROPERTIES OF SHAPES

## PARALLELOGRAM

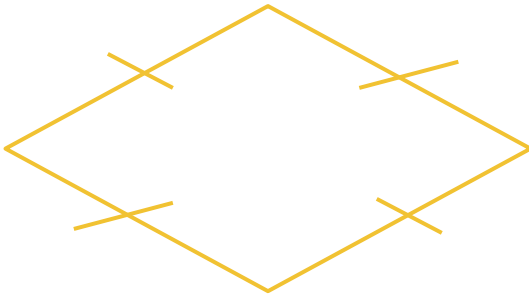


Parallelogram is a quadrilateral with:



- two pairs of parallel sides
- equal opposite sides
- opposite angles are equal

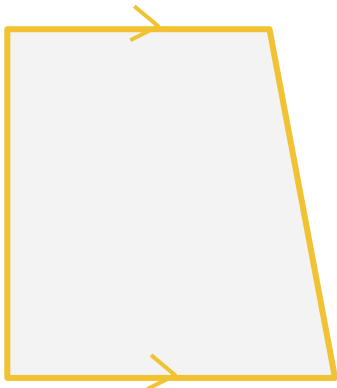
## RHOMBUS



Rhombus is a parallelogram with:

- four equal sides
- Opposite sides are parallel
- Opposite angles are equal
- Diagonals bisect each other at right angle

## TRAPEZOID



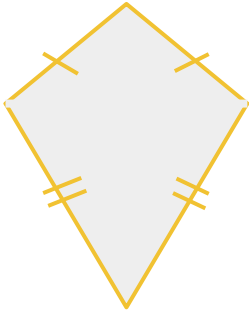
Trapezoid is a quadrilateral with:

- one pair of opposite parallel sides



# PROPERTIES OF SHAPES

## KITE



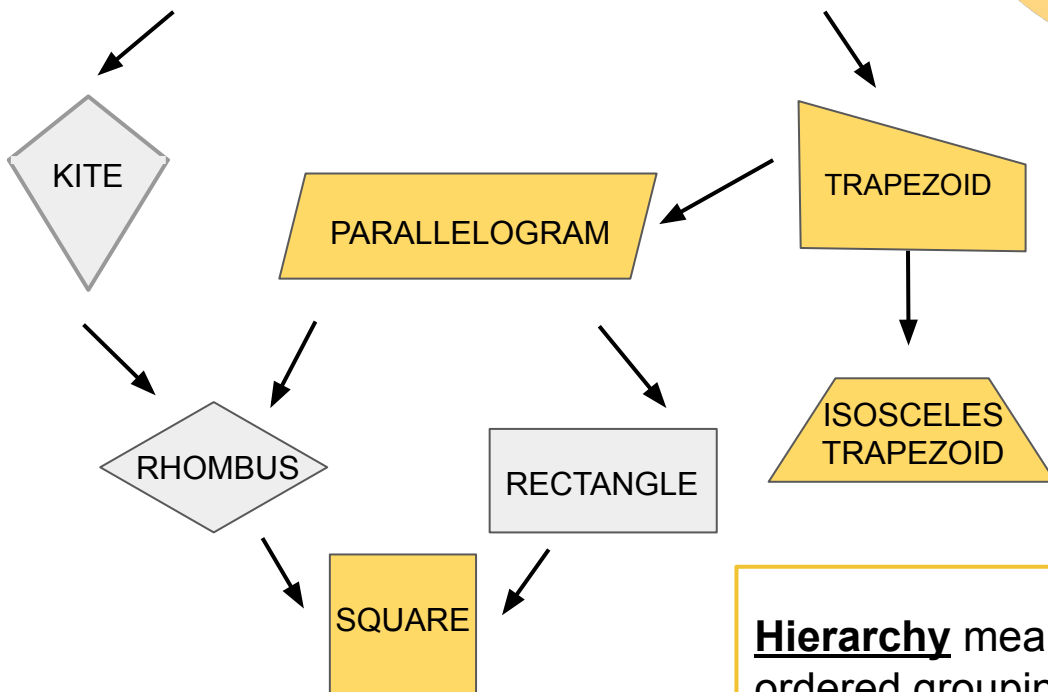
Kite is a quadrilateral with:

- two pairs of adjacent sides of the same length
- One pair of opposite sides are equal
- One diagonal bisects the other
- Diagonals intersect at right angle

# HIERARCHY OF SHAPES



## QUADRILATERAL



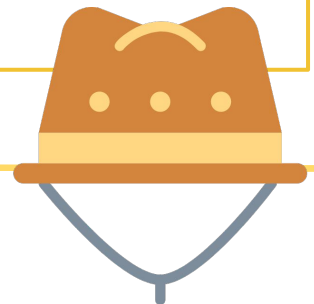
**Hierarchy** means series of ordered grouping of shapes



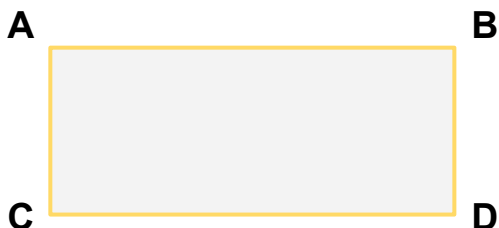
## HIERARCHY OF SHAPES

### So what does hierarchy of quadrilaterals say?

- ❑ Kite is a quadrilateral.
- ❑ Trapezoid is a quadrilateral.
- ❑ A rhombus is a type of kite. It is also a kind of parallelogram.
- ❑ Parallelogram is a type of trapezoid.
- ❑ Rectangle is a parallelogram and at the same time, an isosceles trapezoid. It possesses the properties of both parallelogram and isosceles trapezoid.
- ❑ Square has the properties of parallelogram, rhombus, and rectangle.



## ILLUSTRATIVE EXAMPLES



ABCD is a rectangle. AB measures 12 in. If  $AC = \frac{1}{2}$  of AB, compute for the area and perimeter of ABCD.

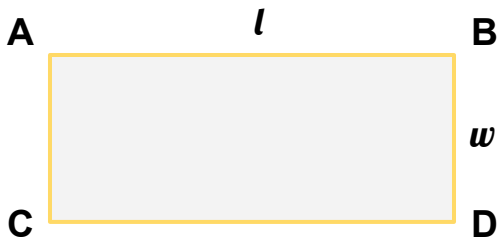
Let first solve the measurement of AC. Since AC is just a half of AB, then  $\frac{1}{2}$  of 12 is 6. Thus,  $AC = 6$ .

### REMEMBER:

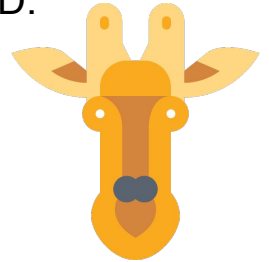
One of the properties of rectangle is that its opposite sides are equal. AB and CD are opposite sides. Thus, their length is equal. Likewise, AC and BD are opposite sides so their lengths are equal as well.



## ILLUSTRATIVE EXAMPLES



ABCD is a rectangle. AB measures 12 in. If  $AC = \frac{1}{2}$  of AB, compute for the area and perimeter of ABCD.



$$AB = 12 \text{ in} \\ AC = 6 \text{ in}$$

$$CD = 12 \text{ in} \\ BD = 6 \text{ in}$$

Perimeter of rectangle ABCD

$$P = 2L + 2W$$

$$P = 2(12) + 2(6) \text{ in}$$

$$P = 24 + 12 \text{ in}$$

$$P = 36 \text{ in}$$

Thus, the perimeter of rectangle ABCD is 36 inches.

Area of rectangle ABCD

$$A = L \times W$$

$$A = 12 \text{ in} \times 6 \text{ in}$$

$$A = 72 \text{ sq. in}$$

Thus, the area of rectangle ABCD is 72 sq. inches.

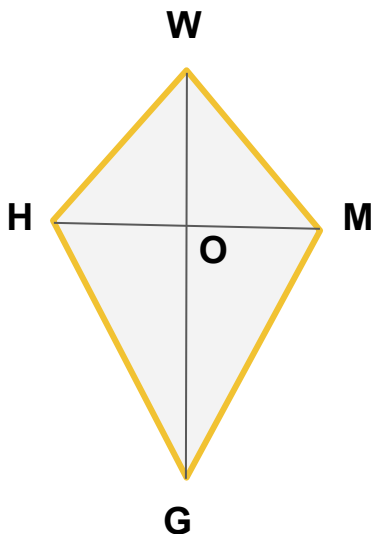
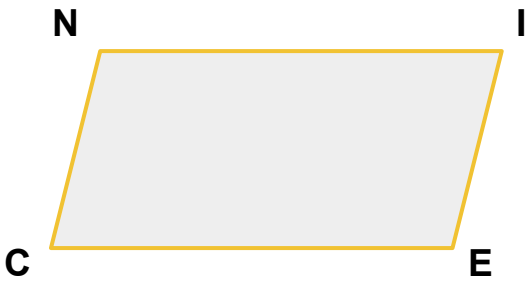


Figure HWMG is a kite. HM and GW are kite's diagonals. Find the measurement of angle MOW.

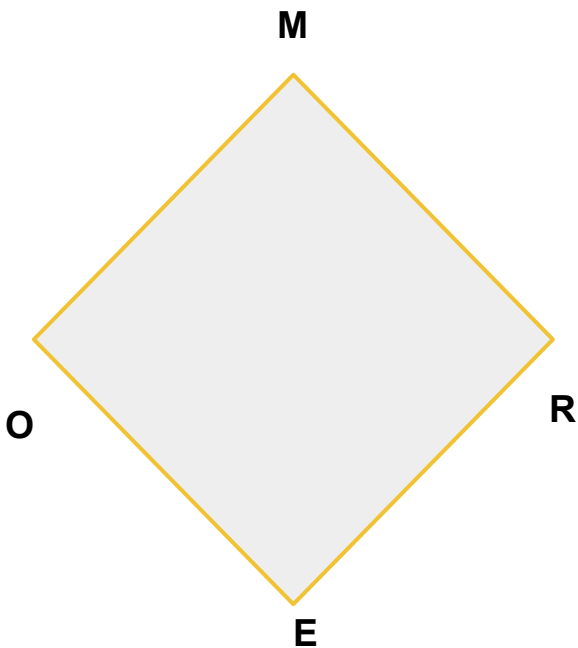
One of the properties of Kite is that: diagonals intersect at right angle. **Thus, angle MOW measures 90 degrees. It is a right angle.**



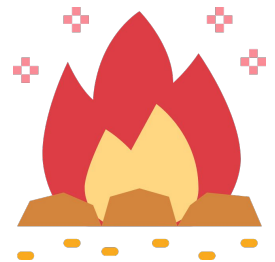
## PRACTICE EXERCISES



NICE is a parallelogram. If NC measures 15 ft and CE measures 23 ft, what is the measure of EI and NI?



MORE is a rhombus. Enumerate which pairs of sides are parallel and equal.



# TABLE OF ACTIVITIES

1. Welcome to the Jungle
2. Riding the Jungle Jeep
3. The Explorer Hat
4. King of the Jungle
5. Forest Map
6. Compass Point
7. The Elephant Tusk
8. Meet the Giraffe
9. Campfire
10. It's Time for Africa





# WELCOME TO THE JUNGLE

Welcome to the jungle! Witness the beauty and diversity of this place by identifying the shape being described.

This is a quadrilateral whose opposite sides are equal and parallel and the opposite angles are equal.

1. \_\_\_\_\_

A parallelogram whose opposite sides are equal and parallel. All of its angles are right.

2. \_\_\_\_\_

A parallelogram whose all sides are parallel and equal. All angles measure 90 degrees.

3. \_\_\_\_\_

A parallelogram whose opposite sides are parallel, all sides and opposite angles are equal Its diagonals bisect each other.

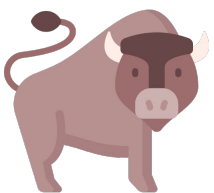
4. \_\_\_\_\_

A quadrilateral whose a pair of opposite sides are parallel.

5. \_\_\_\_\_

A quadrilateral with two pairs of equal adjacent sides, a pair of equal opposite sides

6. \_\_\_\_\_



# RIDING THE JUNGLE JEEP

Have a ride on this jeep to visit the jungle animals. You need to decide first whether the following statements are always, sometimes, or never TRUE.

1. Trapezoid is a parallelogram.

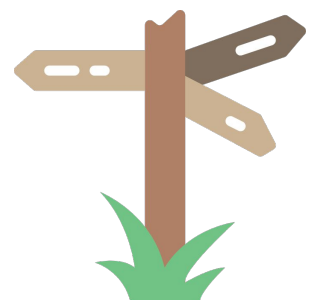
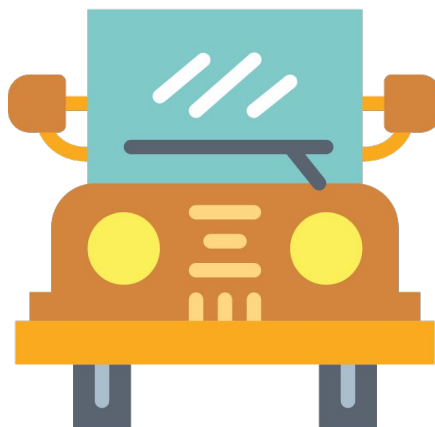
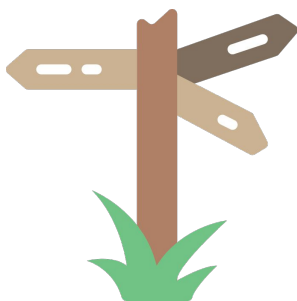
2. Parallelogram is a trapezoid.

3. Rhombus is a kite.

4. Square is a quadrilateral.

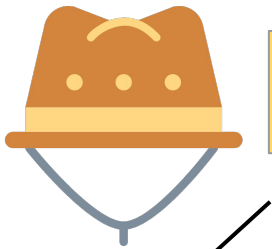
5. A rectangle is a square.

6. A parallelogram is a kite.

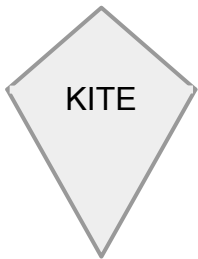


# THE EXPLORER HAT

Be an explorer by completing the hierarchy of shapes chart. As you write the names of the quadrilaterals, give two properties of the indicated shape. Make sure to do it perfectly.



QUADRILATERAL



1.

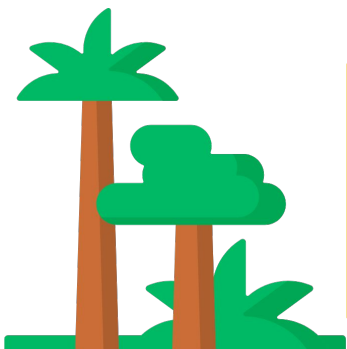
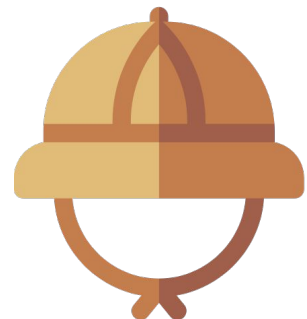


2.

3.

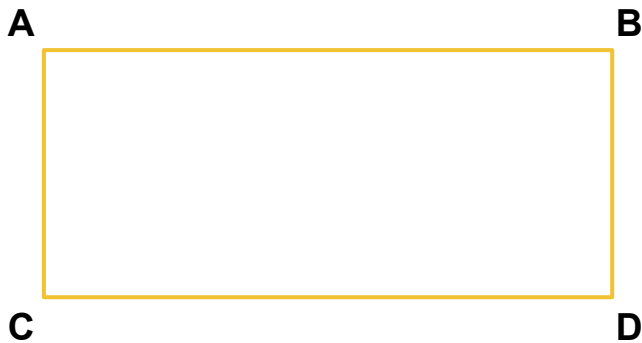
4.

5.



# KING OF THE JUNGLE

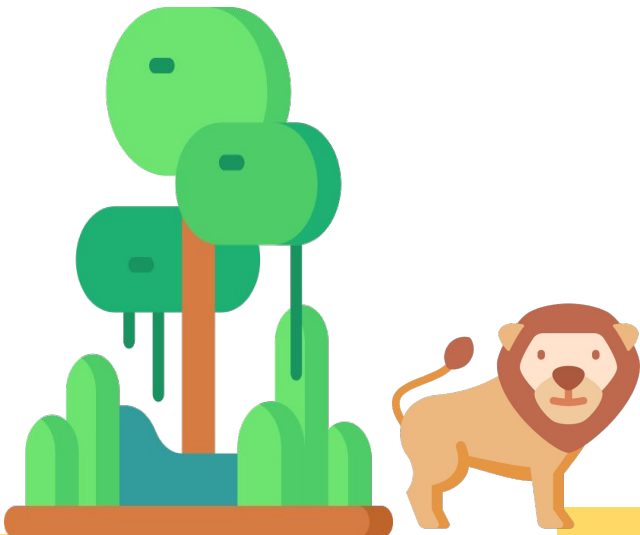
Meet the King of the Jungle by exploring the properties of rectangle.



1. Put tick marks and other symbols on rectangle ABCD to show its properties.

2. In a given rectangle, AB is four times as long as BC. If BC is 4.5 ft, what is the perimeter and area of the rectangle.

3. What is the sum of the angles of rectangle? Explain its properties that you used to answer this question.



# FOREST MAP

Discover what the forest map leading us to! Do it by answering some exercises regarding square.

1. What is the perimeter and area of a square whose side measures 22.5 in?

2. If the perimeter of a square is 72 cm, compute for its area.

3. What will happen to the area of a square if its side is doubled? Provide an example.

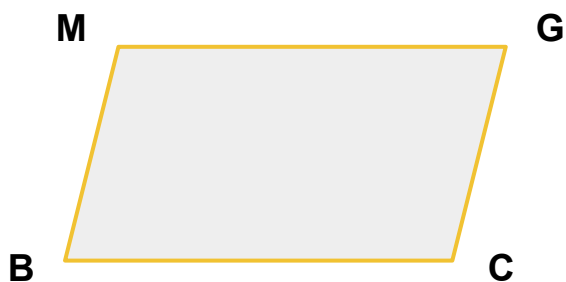
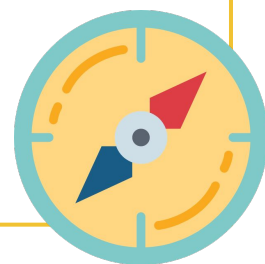
4. What will happen to the perimeter of a square if its side is tripled? Provide an example.



# COMPASS POINT

Which direction is it pointing? Find it out while dealing with parallelograms.

1. Create parallelogram whose dimensions are 10 cm and 12 cm, respectively. Put proper marks/labels to indicate its properties.



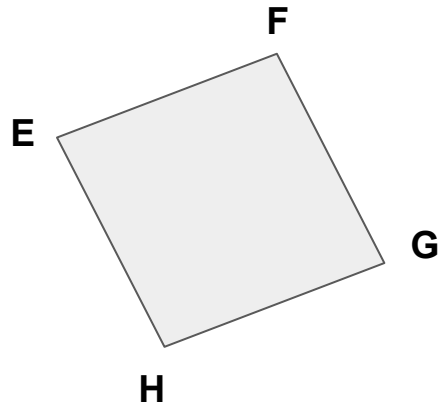
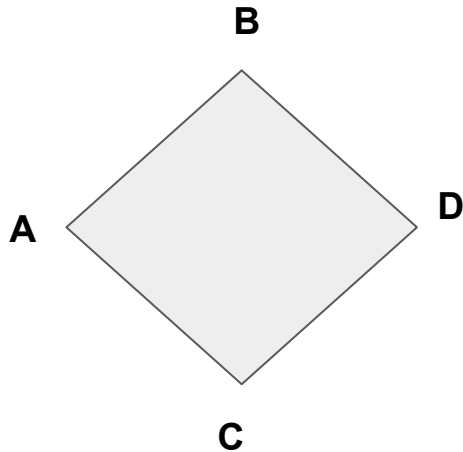
2. MGBC is a parallelogram. If angle BMG is  $88^\circ$ , what is the measurement of angle BCG?

3. If angle CGM measures  $110^\circ$ , find the measures of the remaining three angles.



# THE ELEPHANT TUSK

Take care of the elephant's task by completing these tasks involving rhombuses.



1. A. Which side is parallel to AB? \_\_\_\_\_

B. Which angle has the same measure with  $\angle B$ ?

\_\_\_\_\_

C. Is  $m\angle C = m\angle D$ ? Why or why not?

\_\_\_\_\_

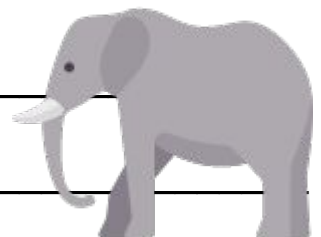
2. A. If EF is 15 units, then GH is \_\_\_\_\_

B.  $m\angle F = 85^\circ$ , what is  $m\angle G$ ? \_\_\_\_\_

C. Is EF parallel to GH? Why or why not?

\_\_\_\_\_

\_\_\_\_\_



# MEET THE GIRAFFE

Look at the giraffe! It needs help to eat his food. Help him out by applying your understanding about trapezoid.

1. PQRS is a trapezoid. PQ has the same length with RS. What type of trapezoid is PQRS? Why?

---

---

---

---

---

2. Illustrate trapezoid PQRS. Make sure to include proper labels of its properties.

3. What makes a trapezoid a unique type of polygon?

---

---

---

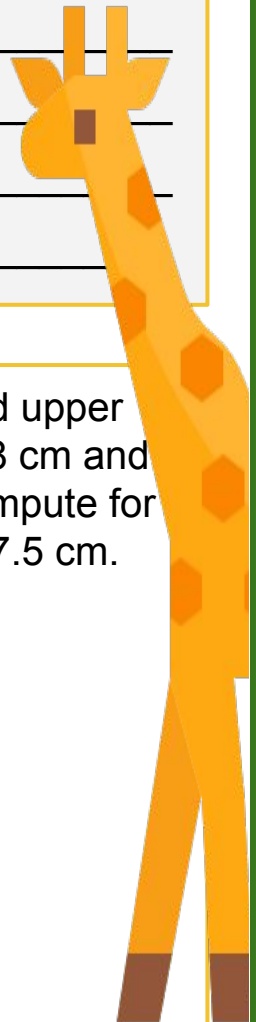
---

---

---

---

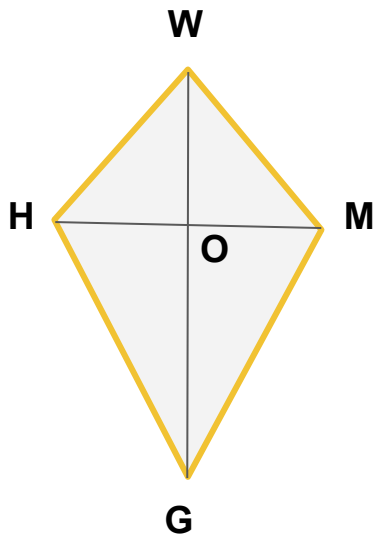
4. If the lower base and upper base of a trapezoid is 8 cm and 12 cm respectively, compute for its area given that  $h = 7.5$  cm.





# CAMPFIRE

Keep the fire burning as you explore the properties of kite.



## TRUE or FALSE?

\_\_\_\_\_ 1.  $HW = MW$

\_\_\_\_\_ 2.  $HG = WM$

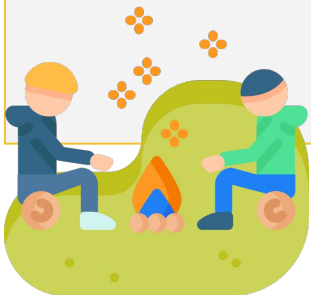
\_\_\_\_\_ 3.  $m\angle GHW = m\angle GMW$

\_\_\_\_\_ 4.  $m\angle HWG = m\angle MWG$

\_\_\_\_\_ 5.  $m\angle HOG = 90^\circ$

6. If  $m\angle WOM = 90^\circ$ , what is the measurement of angle WOH, HOG, and MOG?

7. If HG is twice the length of HW, and  $MW = 11.5$  cm, find the measurement of HG and HW.



# IT'S TIME FOR AFRICA

**Make way for Africa by having the most diverse safari in the world!  
Accomplish these tasks!**

1. A quadrilateral has the following angle measures:  $135^\circ$ ,  $55^\circ$ , and  $20^\circ$ . What is the measurement of the fourth angle? Illustrate the given with angle measures.



2. Compare rectangle and trapezoid based on their properties.

3. Which statement is TRUE? A square is a rectangle or a rectangle is a square. Justify your answer.



# ANSWER GUIDE

## Activity 1

- |                  |              |           |
|------------------|--------------|-----------|
| 1. Parallelogram | 2. Rectangle | 3. Square |
| 4. Rhombus       | 5. Trapezoid | 6. Kite   |

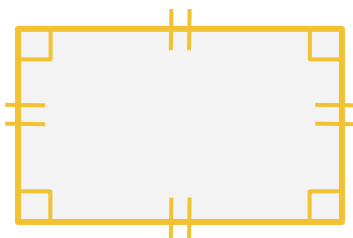
## Activity 2

- |          |              |              |    |
|----------|--------------|--------------|----|
| 1. NEVER | 2. SOMETIMES | 3. SOMETIMES | 4. |
| ALWAYS   | 5. NEVER     | 6. NEVER     |    |

## Activity 3

- |                        |            |              |
|------------------------|------------|--------------|
| 1. Parallelogram       | 2. Rhombus | 3. Rectangle |
| 4. Isosceles trapezoid | 5. Square  |              |

## Activity 4



2. Perimeter =  $2L + 2W = 2(4.5) + 2(18) = 9 + 36 = 45$  ft

Area =  $LW = (4.5) \times (18) = 81$  sq. ft

3. 360 degrees because all of the four angles are right. When you get the sum of these four angles, the answer is 360 degrees.

## Activity 5

1. Perimeter =  $4S = 4(22.5) = 90$  in Area =  $s \times s = 22.5 \times 22.5 = 506.25$  sq. in

2.  $P = 72$  cm. To get the length of the side, divide 72 by 4.  $S = 18$ .

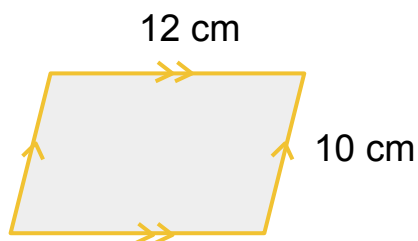
Area =  $s \times s = 18 \times 18 = 324$  sq. cm

3. The area will increase four times. 4. The perimeter will be tripled.



# ANSWER GUIDE

## Activity 6

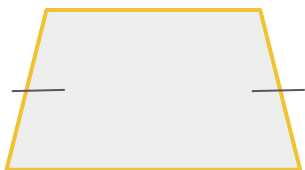


2. 88 degrees      3. Angle CMB = 110 degrees, angle CGM = 80 degrees, angle CBM = 80 degrees

## Activity 7

1. A. CD      B. angle C      C. No. they are not opposite angles  
2. A. 15 units      B. angle G = 95 degrees      C. Yes because they are opposite sides.

## Activity 8



1. Isosceles trapezoid because it has a pair of sides that are equal in measure.  
3. It has one pair of opposite sides that is parallel  
4. 75 sq. cm

## Activity 9

1. TRUE    2. FALSE    3. TRUE    4. TRUE    5. TRUE  
6. 90 degrees as well    7. HG = 30 cm and HW = 11.5 cm

## Activity 10

1. 150 degrees    2. Rectangle is a parallelogram whose opposite sides are equal. Its angles are all right. Trapezoid has only one pair of opposite sides parallel.  
3. A square is a rectangle because based on the hierarchy, square has the properties of rectangle.



# Copyright Notice

This resource is licensed under the [Creative Commons Attribution-NonCommercial 4.0](https://creativecommons.org/licenses/by-nc/4.0/) International license.

You are free to:

- **Share** – copy and redistribute the material in any medium or format
- **Adapt** – remix, transform, and build upon the material

Under the following terms:

- **Attribution** – You must give appropriate credit, provide a link to the license, and indicate if changes were made. You may do so in any reasonable manner, but not in any way that suggests the licensor endorses you or your use.
- **NonCommercial** – You may not use the material for commercial purposes.

For more information on this license, visit the following link:

<http://creativecommons.org/licenses/by-nc/4.0/>

Where possible, free-use images are sourced from online repositories such as Wikipedia and Wikimedia Commons. References and sources for images are provided in the speaker notes section of this document.

Thank you!



# Thank you

Thank you so much for purchasing and downloading this resource.

We hope it has been useful for you in the classroom and that your students enjoy the activities.

For more teaching and homeschooling resources like this, don't forget to [come back](#) and download the new material we add every week!

Thanks for supporting **Helping With Math**. We can provide teachers with low-cost, high-quality teaching and homeschooling resources because of our loyal subscribers and hope to serve you for many years to come.

- The Entire Helping With Math Team :)

